



# NIMCET

# Previous year paper 2015

## Included Subjects

Mathematics

Logical Reasoning

Computer

English

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#### Mathematics:

1. A professor has 24 text books on computer science and is concerned about their coverage of the topics (P) compilers, (Q) data structures and (R) operating systems. The following data gives the number of books that contains material on these topics:  $n(P) = 8, n(Q) = 13, n(R) = 13, n(P \cap Q) = 3, n(P \cap Q \cap R) = 2$ , where  $n(x)$  is the cardinality of the set  $x$ . Then, the number of text books that have no compiler is  
(A) 4 (B) 8  
(C) 12 (D) 16
2. The value of  $\tan\left(\frac{7\pi}{8}\right)$  is  
(A)  $1 - \sqrt{2}$  (B)  $1 + \sqrt{2}$   
(C)  $\sqrt{2} + \sqrt{3}$  (D)  $\sqrt{2} - \sqrt{3}$
3. If  $a$  and  $b$  are vectors such that  $|a| = 13, |b| = 5$  and  $a \cdot b = 60$ , then the value of  $|a \times b|$  is  
(A) 625 (B) 225  
(C) 45 (D) 25
4. Two towers face each other separated by a distance of 25 m. As seen from the top of the first tower, the angle of depression of the second tower's base is  $60^\circ$  and that of the top is  $30^\circ$ . The height (in meters) of the second tower is  
(A)  $\frac{50}{\sqrt{3}}$  (B)  $\frac{25}{\sqrt{3}}$   
(C) 50 (D)  $25\sqrt{3}$
5. If  $a = 4\hat{i} + 6\hat{j}$  and  $b = 3\hat{i} + 4\hat{k}$ , then the vector form of the component of  $a$  along  $b$  is  
(A)  $\frac{18}{10\sqrt{3}}(3\hat{i} + 4\hat{k})$  (B)  $\frac{18}{5}(3\hat{i} + 4\hat{k})$   
(C)  $\frac{18}{\sqrt{13}}(3\hat{i} + 4\hat{k})$  (D)  $(3\hat{i} + 4\hat{k})$
6. The value of  $\sin^{-1} \frac{1}{\sqrt{2}} + \sin^{-1} \frac{\sqrt{2}-\sqrt{1}}{\sqrt{6}} + \sin^{-1} \frac{\sqrt{3}-\sqrt{2}}{\sqrt{12}} + \dots$  to infinity is equal to  
(A)  $\pi$  (B)  $\frac{\pi}{3}$   
(C)  $\frac{\pi}{2}$  (D)  $\frac{\pi}{4}$
7. If two circle  $x^2 + y^2 + 2gx + 2fy = 0$  and  $x^2 + y^2 + 2g'x + 2f'y = 0$  touch each other, then which of the following is true?  
(A)  $gf = gf'$  (B)  $g'f = gf'$   
(C)  $gg' = ff'$  (D) None of these
8.  $\int_0^\pi [\cot x] dx$ , where  $[.]$  denotes the greatest integer function, is equal to  
(A)  $\frac{\pi}{2}$  (B) 1  
(C) -1 (D)  $-\frac{\pi}{2}$
9. In a right-angled triangle, the hypotenuse is four times the perpendicular drawn to it from the opposite vertex. The value of one of the acute angle is  
(A)  $45^\circ$  (B)  $30^\circ$   
(C)  $15^\circ$  (D) None of these
10. A targeting B, B and C are targeting A, probability of hitting the target by A, B and C are  $\frac{2}{3}, \frac{1}{2}$  and  $\frac{1}{3}$  respectively. If A is hit, then the probability that B hit the target and does not, is  
(A)  $\frac{1}{2}$  (B)  $\frac{1}{3}$   
(C)  $\frac{2}{3}$  (D)  $\frac{3}{4}$
11. If the angles of a triangle are in the ratio 2 : 3 : 7, then the ratio of the sides opposite to these angles is  
(A)  $\sqrt{2} : 2 : \sqrt{3} + 1$  (B)  $2 : \sqrt{2} : \sqrt{3} + 1$   
(C)  $2 : \sqrt{2} : \frac{\sqrt{2}}{\sqrt{3}-1}$  (D)  $\frac{1}{\sqrt{2}} : 2 : \frac{\sqrt{3}+1}{2}$
12. Suppose that, A and B are two events with probabilities  $P(A) = \frac{1}{2}, P(B) = \frac{1}{3}$ . Then, which of the following is true?  
(A)  $\frac{1}{3} \leq P(A \cap B) \leq \frac{1}{2}$  (B)  $\frac{1}{4} \leq P(A \cap B) \leq \frac{1}{3}$   
(C)  $\frac{1}{6} \leq P(A \cap B) \leq \frac{1}{3}$  (D)  $\frac{1}{4} \leq P(A \cap B) \leq \frac{1}{2}$
13. The number of one-to-one function from  $\{1, 2, 3\}$  to  $\{1, 2, 3, 4, 5\}$  is





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(A) 125  
(C) 10

(B) 243  
(D) 60

14. A harbour lies in a direction  $60^\circ$  South of West from a fort and at a distance 30 km from it, a ship sets out from the harbour at noon and sail due East at 10 km an hour. The time at which the ship will be 70 km from the fort is

(A) 7 PM (B) 8 PM  
(C) 5 PM (D) 10 PM

15. If  $x, y$  and  $z$  are three consecutive positive integers, then  $\log(1 + xz)$  is

(A)  $\log y$  (B)  $\log \frac{y}{2}$   
(C)  $\log(2y)$  (D)  $2 \log(y)$

16. If  $a, b$  and  $c$  are in arithmetic progression, then  $\log_{ax} x, \log_{bx} x$  and  $\log_{cx} x$  are in

(A) arithmetic progression  
(B) geometric progression  
(C) harmonic progression  
(D) arithmetic-geometric progression

17. If  $a$  and  $b$  are vector in space, given by  $a = \frac{i-2j}{\sqrt{5}}$  and  $b = \frac{2i-j+3k}{\sqrt{14}}$ , then the value of  $(2a + b) \cdot [(a \times b) \times (a - 2b)]$  is

(A) 3 (B) 4  
(C) 5 (D) 6

18. The value of the sum  $\frac{1}{2\sqrt{1+1\sqrt{2}}} + \frac{1}{3\sqrt{2+2\sqrt{3}}} + \frac{1}{4\sqrt{3+3\sqrt{4}}} + \dots + \frac{1}{25\sqrt{24+24\sqrt{25}}}$  is

(A)  $\frac{9}{10}$  (B)  $\frac{4}{5}$   
(C)  $\frac{14}{15}$  (D)  $\frac{7}{15}$

19. If  $a = i - \hat{k}, b = x\hat{i} + \hat{j} + (1-x)\hat{k}$  and  $c = y\hat{i} + x\hat{j} + (1+x-y)\hat{k}$ , then  $[a \ b \ c]$  depends on

(A) Neither  $x$  nor  $y$  (B) Only  $x$   
(C) Only  $y$  (D) Both  $x$  and  $y$

20. If  $42({}^nP_2) = {}^nP_4$ , then the value of  $n$  is

(A) 2 (B) 4  
(C) 9 (D) 42

21. Let  $a$  and  $b$  be two vectors. Which of the following vectors are not perpendicular to each other?

(A)  $(a \times b)$  and  $a$

(B)  $(a + b)$  and  $a \times b$

(C)  $(a + b)$  and  $a - b$

(D)  $a - b$  and  $a \times b$

22. If  $A = \begin{bmatrix} a & b & c \\ b & c & a \\ c & a & b \end{bmatrix}$ , where  $a, b$  and  $c$  are real positive numbers such that  $abc = 1$  and  $A^T A = 1$ , then the equation that holds true among the following is

(A)  $a + b + c = 1$  (B)  $a^2 + b^2 + c^2 = 1$   
(C)  $ab + bc + ca = 0$  (D)  $a^3 + b^3 + c^3 = 4$

23. The equation of the tangent at any point of curve  $x = a \cos 2t, y = 2\sqrt{2}a \sin t$ , with  $m$  as its slope is

(A)  $y = mx + a \left(m - \frac{1}{m}\right)$  (B)  $y = mx - a \left(m + \frac{1}{m}\right)$   
(C)  $y = mx + a \left(a + \frac{1}{a}\right)$  (D)  $y = amx + a \left(m - \frac{1}{m}\right)$

24. The locus of the mid-point of all chords of the parabola  $y^2 = 4x$ , which are drawn through its vertex is

(A)  $y^2 = 8x$  (B)  $y^2 = 2x$   
(C)  $x^2 + 4y^2 = 16$  (D)  $x^2 = 2y$

25. The value of  $\lim_{x \rightarrow a} \frac{\sqrt{a+2x} - \sqrt{3x}}{\sqrt{3a-x} - 2\sqrt{x}}$  is

(A)  $\frac{2}{3}$  (B)  $\frac{2}{\sqrt{3}}$   
(C)  $\frac{3\sqrt{3}}{2}$  (D)  $\frac{2}{3\sqrt{3}}$

26. The value of  $\int_{-\pi/3}^{\pi/3} \frac{x \sin x}{\cos^2 x} dx$  is

(A)  $\frac{1}{3}(4\pi + 1)$  (B)  $\frac{4\pi}{3} - 2 \log \tan \frac{5\pi}{12}$   
(C)  $\frac{4\pi}{3} + \log \tan \frac{5\pi}{12}$  (D)  $\frac{4\pi}{3} - \log \tan \frac{5\pi}{12}$

27. The foci of the ellipse  $\frac{x^2}{16} + \frac{y^2}{b^2} = 1$  and the hyperbola  $\frac{x^2}{144} - \frac{y^2}{81} = \frac{1}{25}$  coincide, then value of  $b^2$  is

(A) 1 (B) 5  
(C) 7 (D) 9

28. If  $A + B + C = \pi$ , then the value of

$\begin{vmatrix} \sin(A+B+C) & \sin B & \cos C \\ -\sin B & 0 & \tan A \\ \cos(A+B) & -\tan A & 0 \end{vmatrix}$  is

(A) 0 (B) 1  
(C)  $2 \sin A \sin B$  (D) 2







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29. If the mean deviation of the number  $1, 1 + d, 1 + 2d, \dots, 1 + 100d$  from their mean is 225, then the value of  $d$  is

- (A) 20.0 (B) 10.1  
(C) 20.2 (D) 10.0

30. If  $P = \sin^{20}\theta + \cos^{48}\theta$ , then the inequality that holds for all values of  $\theta$  is

- (A)  $P \geq 1$  (B)  $0 < P \leq 1$   
(C)  $1 < P < 3$  (D)  $0 \leq P \leq 1$

31. The foot of the perpendicular from the point  $(2, 4)$  upon  $x + y = 1$  is

- (A)  $(\frac{1}{2}, \frac{3}{2})$  (B)  $(-\frac{1}{2}, \frac{3}{2})$   
(C)  $(\frac{4}{3}, \frac{1}{3})$  (D)  $(\frac{4}{3}, -\frac{1}{2})$

32. The value of  $k$  for which the equation  $(k - 2)x^2 + 8x + k + 4 = 0$  has both real, distinct and negative roots is

- (A) 0 (B) 2  
(C) 3 (D) -4

33. If  $(2, 1), (-1, -2), (3, 3)$  are the mid-points of the sides  $BC, CA$  and  $AB$  of a triangle  $ABC$ , then equation of the line  $BC$  is

- (A)  $5x + 4y + 6 = 0$  (B)  $5x - 4y - 6 = 0$   
(C)  $5x + 4y - 6 = 0$  (D)  $5x - 4y + 6 = 0$

34. If a fair dice is rolled successively, then the probability that 1 appears in an even numbered throw is

- (A)  $\frac{5}{36}$  (B)  $\frac{3}{11}$   
(C)  $\frac{1}{6}$  (D)  $\frac{5}{11}$

35. Let  $a = \hat{i} + \hat{j} + \hat{k}, b = \hat{i} - \hat{j} + \hat{k}$  and  $c = \hat{i} - \hat{j} - \hat{k}$  be three vectors. A vector  $v$  is in the plane of  $a$  and  $b$  whose projection on  $\frac{c}{|c|}$  is  $\frac{1}{\sqrt{3}}$  is

- (A)  $3\hat{i} - \hat{j} + 3\hat{k}$  (B)  $\hat{i} - 3\hat{j} + 3\hat{k}$   
(C)  $5\hat{i} - 2\hat{j} + 5\hat{k}$  (D)  $2\hat{i} - \hat{j} + 3\hat{k}$

36. The number of bit strings of length 10 that contain either five consecutive 0's or five consecutive 1's is

- (A) 64 (B) 112  
(C) 220 (D) 222

37. If  $0 < x < \pi$  and  $\cos x + \sin x = \frac{1}{2}$ , then the value of  $\tan x$

- (A)  $\frac{4-\sqrt{7}}{3}$  (B)  $\frac{4+\sqrt{7}}{3}$   
(C)  $\frac{1+\sqrt{7}}{4}$  (D)  $\frac{1-\sqrt{7}}{4}$

38. If  $a, b$  and  $c$  are the position vectors of the vertices  $A, B, C$  of a triangle  $ABC$ , then the area of the triangle  $ABC$  is

- (A)  $\frac{1}{2}|a \times b + b \times c + c \times a|$  (B)  $|a \times b|$   
(C)  $\frac{1}{2}|a \times b - b \times c - c \times a|$  (D)  $|a \times (b \times c)|$

39. If  $\int e^x(f(x) - f'(x))dx = \Phi(x)$ , then the value of  $\int e^x f(x)dx$  is

- (A)  $\Phi(x) + e^x f(x)$  (B)  $\Phi(x) - e^x f(x)$   
(C)  $\frac{1}{2}[\Phi(x) + e^x f(x)]$  (D)  $\frac{1}{2}[\Phi(x) + e^x f'(x)]$

40. If  $3x + 4y + K = 0$  is a tangent to the hyperbola  $9x^2 - 16y^2 = 144$ , then the value of  $K$  is

- (A) 0 (B) 1  
(C) -1 (D) -3

41.  $a, b$  and  $c$  are positive integers such that  $a^2 + b^2 - 2bc = 100$  and  $2ab - c^2 = 100$ . Then, the value of  $\frac{a+b}{c}$  is

- (A) 10 (B) 100  
(C) 2 (D) 20

42. If  $(-4, 5)$  is one vertex and  $7x - y + 8 = 0$  is one diagonal of a square, then the equation of the other diagonal is

- (A)  $x + 7y = 21$  (B)  $x + 7y = 31$   
(C)  $x + 7y = 11$  (D)  $x + 7y = 35$

43. Out of  $2n + 1$  tickets, which are consecutively numbered three are drawn at random. Then, the probability that, the numbers on them are in arithmetic progression is

- (A)  $\frac{n^2}{4n^2-1}$  (B)  $\frac{n}{4n^2-1}$   
(C)  $\frac{3n^2}{4n^2-1}$  (D)  $\frac{3n}{4n^2-1}$

44. A circle touches the  $X$ -axis and also touches another circle with centre at  $(0, 3)$  and radius 2. Then, the locus of the centre of the first circle is





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(A) a parabola  
(C) a circle

(B) a hyperbola  
(D) an ellipse

45. Let  $\bar{P}$  and  $\bar{Q}$  denote the complements of two sets  $P$  and  $Q$ . Then, the set  $(P - Q) \cup (Q - P) \cup (P \cap Q)$  is

(A)  $P \cup Q$   
(C)  $P \cap Q$

(B)  $\bar{P} \cup \bar{Q}$   
(D)  $\bar{P} \cap \bar{Q}$

46. With the usual notation  $\frac{d^2x}{dy^2}$  is

(A)  $\left(\frac{d^2y}{dx^2}\right)^{-1}$

(B)  $\frac{d^2y}{dx^2} \left(\frac{dy}{dx}\right)^{-2}$

(C)  $-\left(\frac{d^2y}{dx^2}\right)^{-1} \left(\frac{dy}{dx}\right)^{-2}$

(D)  $-\left(\frac{d^2y}{dx^2}\right) \left(\frac{dy}{dx}\right)^{-2}$

47. The radius of the circle passing through the foci of the ellipse  $\frac{x^2}{16} + \frac{y^2}{9} = 1$  and having its centre at  $(0, 3)$  is

(A) 4 units

(B) 3 units

(C)  $\sqrt{12}$  units

(D)  $\frac{7}{2}$  units

48. A function  $F: (0, \pi) \rightarrow R$  defined by  $f(x) = 2 \sin x + \cos 2x$  has

(A) a local minimum but no local maximum

(B) a local maximum but no local minimum

(C) Both local minimum and local maximum

(D) Neither a local minimum nor a local maximum

49. A matrix  $M_r$  is defined as  $M_r =$

$\begin{bmatrix} r & r-1 \\ r-1 & r \end{bmatrix}$   $r \in N$ , then the value of  $\det(M_1) + \det(M_2) + \dots + \det(M_{2015})$  is

(A)  $2014^2$

(B)  $2013^2$

(C) 2015

(D)  $2015^2$

50. If  $AC = 2\hat{i} + \hat{j} + \hat{k}$  and  $BD = -\hat{i} + 3\hat{j} + 2\hat{k}$ , then the area of the quadrilateral  $ABCD$  is

(A)  $\frac{5}{2}\sqrt{3}$

(B)  $5\sqrt{3}$

(C)  $\frac{15}{2}\sqrt{3}$

(D)  $10\sqrt{3}$

## Reasoning/Aptitude:

**Directions [Q. Nos. 51-54]** A circular field with inner radius of 10m and outer radius of 20 m is divided into 5 successive stages for ploughing. The ploughing at each stage with starting points  $P_1, P_2, P_3, P_4$  and  $P_5$  was allotted to one of the five farmers  $F_1, F_2, F_3, F_4$  and  $F_5$  not necessarily in that order.

- $F_5$  was allotted the stage starting a point  $P_4$ .
- The stage from  $P_5$  to  $P_3$  was not the first stage.
- $F_4$  was allotted the work of the fourth stage.
- Finishing point of stage 3 was  $P_1$  and the work was not allotted to  $F_1$ .
- $F_3$  was allotted the work of stage ending at  $P_5$ .

51. Which of the following is the finish point for farmer  $F_2$ ?

(A)  $P_1$

(B)  $P_2$

(C)  $P_3$

(D)  $P_4$

52. Which stage was ploughed by  $F_5$ ?

(A) 2

(B) 3

(C) 4

(D) 5

53. What are the starting and ending points of the field ploughed by  $F_4$ ?

(A)  $P_1$  and  $P_2$

(B)  $P_1$  and  $P_4$

(C)  $P_4$  and  $P_2$

(D)  $P_2$  and  $P_4$

54. What is the starting point for stage 3?

(A)  $P_2$

(B)  $P_3$

(C)  $P_4$

(D) Cannot be determined

55. If Tuesday falls on the fourth of a month, then which day will fall three days after 24th of the same month?

(A) Monday

(B) Tuesday

(C) Thursday

(D) Friday

56. If the statements "All chickens are birds", "Some chickens are hens" and "Female birds lay eggs", are all facts, then which of the following must also be a fact?

I. All birds lay eggs

II. Some hens are birds

III. Some chickens are not hens

(A) I and II

(B) II and III

(C) I and III

(D) Neither I nor II nor III





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### Directions [Q. Nos. 57-60]

- There is a family of six member A, B, C, D, E and F.
- There are two married couples in the family and the family members represent three generations.
- Each member has a distinct choice of a colour amongst Green, Yellow, Black, Red, White and Pink.
- No lady member likes either Green or White.
- C, who likes Black colour, is the daughter-in-law of E.
- B is the brother of F and son of D and likes Pink.
- A is the grandmother of F and F does not like Red.
- Wife of the husband having a choice for Green colour likes Yellow.

57. Which of the following is the colour preference of A?

- (A) Red (B) Yellow  
(C) Either Red or Yellow (D) Cannot be determined

58. Which of the following could be the colour combination of one of the couples?

- (A) Yellow-Red (B) Green-Black  
(C) Red-Yellow (D) Yellow-Green

59. Which of the following is one of the married couples?

- (A) CD (B) AC  
(C) AD (D) Cannot be Determined

60. Which of the following is true about F?

- (A) Brother of B (C) Sister of B  
(C) Daughter of C (D) Cannot be determined

61. If the English word "EXAMINATION" is coded as 56149512965, then the word "GOVERNMENT" is coded as

- (A) 7645954552 (B) 7654694562  
(C) 7645955423 (D) 7654964526

62. Gopal starts from his house towards West. After Walking a distance 30 m, he turned towards right and walked 20 m. He turned left and after moving a distance of 10 m, turned to his left again and walked 40 m. Then, he turned left and walked 5 m. Finally, he turns to his left. In Which Direction is the walking

now?

- (A) North (B) South  
(C) East (D) South East

63. Read the conclusion and then decide which of the given conclusions logically follows from the two given statements (i) and (ii) disregarding commonly known facts.

### Statements

- (i) No women Teacher can play.  
(ii) Some women teachers are athletes

### Conclusions

- I. Male athletes can play.  
II. Some athletes can play.  
(A) Only Conclusion I follows  
(B) Only Conclusions II follows  
(C) Either I or II follows  
(D) Neither I nor II follows

64. Which of the following come next in the series 8, 6, 9, 23, 87, .....?

- (A) 28 (B) 226  
(C) 324 (D) 429

65. In an examination there are 100 questions divided into 3 parts A, B and C and each part should contain at least one question. Each question in parts A, B and C carry 1, 2 and 3 marks respectively. Part A is for at least 60% of the total marks and part B should contain 23 questions. How many questions must be set in part C?

- (A) 1 (B) 2  
(C) 3 (D) Cannot be determined

66. If  $\div$  means addition,  $-$  means division,  $\times$  means subtraction and  $+$  means multiplication, then the value of  $\frac{(36 \times 4) - 8 \times 4}{4 + 8 \times 2 + 16 \div 1}$  is

- (A) 0 (B) 8  
(C) 12 (D) 16

67. Which letter is the word CYBERNETICS occupies the same position as it does in the English alphabet?

- (A) C (B) E  
(C) I (D) T







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68. The remainder when  $2^{31}$  is divided by 5 is

- (A) 1 (B) 2  
(C) 3 (D) 4

**Directions [Q. Nos. 69-70]** The letter of the English alphabet from A to M were written, leaving space for one letter between every two letters and then the remaining letters were inserted beginning with N and ending the series with Z after M.

69. Which letter would be 3rd to the right of the 7th letter from the left?

- (A) C (B) O  
(C) R (D) S

70. Which letter would be exactly in the middle of eighteenth letter from the beginning and fifteenth from the end?

- (A) G (B) H  
(C) J (D) L

71. How many 3-digit numbers divisible by 5, can be formed using the digits 2, 3, 5, 6, 7 and 9, without repetition of digits?

- (A) 216 (B) 20  
(C) 120 (D) 24

72. Using only 2, 5, 10, 25, and 50 paise coins, what is the smallest number of coins required to pay exactly 78 paise, 69 paise and ₹1.01 to three different persons?

- (A) 19 (B) 20  
(C) 17 (D) 18

73. Which of the following two patterns will fit in the blacks of the series  $ZA_5, Y_4B, XC_6, W_3D, \dots$ ?

- (A)  $VE_7$  and  $U_2E$  (B)  $V_2E$  and  $U_7F$   
(C)  $VE_7$  and  $U_2F$  (D)  $VF_7$  and  $U_2E$

74. Which of the following numbers comes next in the two-digit decimal number sequence 61, 52, 63, 94, .....?

- (A) 65 (B) 64  
(C) 56 (D) 46

75. Three ladies X, Y and Z marry three man A, B and C. X is married to A, Y is not married to an engineer. Z is not married to a doctor, C is not a doctor and A is a lawyer. Then, which of the following statements is

correct?

- (A) X is married to a doctor  
(B) Y is married to C, who is a doctor  
(C) Z is married to C, who is an engineer  
(D) None of the above

76. There are five books A, B, C, D and E placed on a table. If A is placed below E, C is placed D, B is placed below A and D is placed between A and E, then which of the following books can be on the top?

- (A) D or E (B) C or E  
(C) A or E (D) None of these

77. Among five children A, B, C, D and E, B is taller than E but shorter than D. A is shorter than C but taller than D. If all the children stand in a line according to their heights, then who would be the fourth if counted from the tallest one?

- (A) D (B) C  
(C) B (D) A

**Directions [Q. Nos. 78-81]**

- In a family of six person A, B, C, D, E and F there are two married couples.
- D is grandmother of A and mother B.
- C is wife of B and mother F.
- F is the granddaughter of E.

78. What is C to A?

- (A) Daughter (B) Grandmother  
(C) Mother (D) Cannot be determined

79. How many male members are there in the family?

- (A) Two (B) Three  
(C) Four (D) Cannot be determined

80. Who among the following is one of the couples?

- (A) CD (B) DE  
(C) EB (D) Cannot be determined

81. Which of the following is true?

- (A) A is brother of F (B) A is sister of F  
(C) B has two daughters (D) None of these





# ACME ACADEMY

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**Directions [Q. Nos. 82-85]** A, B, C, D, E, F and G are seven girls having different amount of money from among ₹ 10, 20, 40, 60, 80, 120 and 200 with them. They had 3 chocolates, 2 toffees and 2 lollipops together, each other having one of these seven items.

- B and F do not have chocolates and they have ₹ 200 and ₹ 80, respectively.
- C has ₹ 60 with her and G has an amount which neither ₹ 40 nor ₹ 120.
- A has ₹ 10 and does not have a toffee.
- The girl having ₹ 40 with her is the only one other than A to have the same type of item.
- E and girl having ₹ 20 with her have the same kind of item.

**82.** How much amount does G have with her?

- (A) ₹ 20 (B) ₹ 10  
(C) ₹ 60 (D) None of these

**83.** Which of the following girls have chocolates with them?

- (A) F, C, G (B) C, G, E  
(C) C, G, D (D) G, D, E

**84.** Which of the following combination is definitely correct?

- (A) C-chocolate ₹ 60 (B) G-toffee- ₹ 20  
(C) C-chocolate- ₹ 40 (D) None of these

**85.** Which girl has ₹ 40 with her?

- (A) E (B) A  
(C) D (D) None of these

**86.** P, Q, R, S, T, U and V are sitting in a row facing North. In order to determine, who is sitting exactly

in the middle of the row, which of the following information is needed?

- I. T and U are sitting at extreme ends of the row.  
II. S is third to the right of T  
III. Q is four places to the left of R and P is two places of the left of V.

- (A) I and II only are sufficient  
(B) I and III only are sufficient  
(C) I and either II or III are sufficient  
(D) I, II and III

**87.** How many times do the hour and the minute hands of a clock overlap in 24h?

- (A) 24 (B) 22  
(C) 26 (D) 20

**88.** In a certain code, TOGETHER is coded as RQEGRJECT. In the same code, PAROLE will be written as

- (A) NCPQJG (B) NCQPJG  
(C) RCPQJK (D) RCTQNG

**89.** A drawer contains 10 black and 10 brown socks which are all mixed up. What is the smallest number of socks to be taken from the drawer to decided without seeing them, to be sure that there is at least one pair of the same colour?

- (A) 11 (B) 10  
(C) 3 (D) Cannot be determined

**90.** Find the missing number in the series: 4, 7, 25, 10, ....., 20, 16, 19

- (A) 13 (B) 15  
(C) 20 (D) 28

## English: ENTRANCE ACADEMY

**91.** Identify the type of error in the sentence: "The cost of this project will be much lesser than 5% more than that predicted earlier".

- (A) syntactical error (B) punctuation error  
(C) grammatical error (D) conflicting words

**92.** Insert appropriate prepositions in the blanks to complete the sentence. "This property has been ..... the possession ..... the royal family ..... generations."

- (A) with, of, of (B) in, of, for  
(C) in, with, by (D) of, by, since

**93.** Choose the right word to fill in the blank in the sentence.

"The mermaid legend ..... have originated with a group of mammals collectively known to science as Srinians".

- (A) should (B) may  
(C) need (D) can







# ACME ACADEMY

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94. Identify appropriate word to fill the blanks in the sentence. "The feeling of guilt left a ..... impression in the life?"

- (A) perennial (B) parenial  
(C) perannial (D) perinial

95. Which of the following sentences is grammatically incorrect?

- (A) He is smiling. (B) He smiles  
(C) He always smiles (D) He is always smiling

96. Find the most suitable phrasal verb to be filled in the following sentence.

"Left too long in the sun, the leaves had all"

- (A) Shrugged off (B) Shared out  
(C) Shrivelled up (D) Skived off

97. Fill in the blank from among the choices in the sentence.

A 'Couch potato' is a person who ....

- (A) spends a lot of time watching television  
(B) spends money on potatoes  
(C) likes potatoes  
(D) is lazy, but intelligent

98. Which of the following sentence is grammatically incorrect?

- (A) She never travelled abroad for fear of becoming ill through eating foreign food  
(B) She avoids foreign travel as she fears she will become ill through eating foreign food  
(C) She never travelled abroad due to her fear of becoming ill through eating foreign food  
(D) She never travelled abroad in fear for becoming ill with eating foreign food

99. Match the most suitable phrasal Verb from Group L to each word in Group M.

Group L		Group M	
1.	Call out	P.	Footballer
2.	Stands in for	Q.	A criminal
3.	Send down	R.	A colleague
4.	Send off	S.	A Doctor

- (A) 3-R, 2-S, 1-P, 4-Q (B) 1-S, 2-R, 3-Q, 4-P  
(C) 1-P, 2-Q, 3-R, 4-S (D) 2-P, 3-S, 4-R, 1-Q

100. Choose the one which best expresses the following sentence in passive/active voice.

"You can play with these kittens quite safely"

- (A) Theses kittens can be played with quite safely  
(B) These kittens can play with you quite safely  
(C) These kittens can be played with you quite safely  
(D) These kittens can played with quite safely

101. Which of the following terms refers to the original inhabitants of a place?

- (A) Originals (B) Aborigines  
(C) Abominables (D) Cannibals

102. Replace the underlined word with one of the choices given without changing the meaning of the sentence. "The news of our success was me with exuberant cries"

- (A) Excited (B) Pathetic  
(C) Exclusive (D) Poignant

103. Select the word that is furthest is meaning to the word AFFLUENCE.

- (A) Stagnation (B) Misery  
(C) Neglect (D) Poverty

### Directions [Q. Nos.104-106]

The proud warrior class of the samurai (meaning "those who serve") grew from a band of mercenaries hired by feudal landowners in the 11<sup>th</sup> century to win them the control of Honshu, Japan's main island. These mercenaries lived by the cult of the sword, worshipping athletic prowess and martial skills. They developed a fierce loyalty to their masters and a fearlessness that made them formidable adversaries. They fought in elaborate armour, wielding their most prized possession, a double-edged sabre with which they could cut a man in half. Later the spartan principles of Zen Buddhism, with its love of nature softened their fighting zeal. It became fashionable for them to live sparse and frugal lives during the Kamakura era (1192-1333), when the ruling warrior family Minamoto moved their seat to power of the eastern city of Kamakura.

104. Who are usually referred to as mercenaries?

- (A) Soldiers with martial skills  
(B) Proud warriors  
(C) Soldiers who fight for money  
(D) Loyal warriors





# ACME ACADEMY

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**105.** Which of the following best describes the warriors?

- (A) Proud, greedy (B) Fearless, worshipful  
(C) Loyal, fearless (D) Possessive, soft

**106.** In the kamakura period it became fashionable for these warriors to live

- (A) Zealour lives (B) Austere lives  
(C) Powerful lives (D) Natural lives

**107.** Rearrange the parts of a sentence referred to by P, Q, R and S to form a complete and meaningful sentence

"I enclose \_ \_ \_ \_ \_".

P: and the postage

Q: a postal order

R: the price of books

S: which will cover

(A) R P S Q

(C) Q S R P

(B) Q S P R

(D) Q P S R

**108.** Which of the following is the antonym of the word 'Exigency'?

- (A) Penchant (B) Emergency  
(C) Earnestness (D) Indifference

**109.** Which of the following prepositions fills up the blanks in the sentence?

"Quinine is an effective antidote ..... Malaria".

- (A) to (B) against  
(C) for (D) None of these

**110.** In the sentence, "The defence labs have showcased many new innovations this year .... there is an error of

- (A) redundancy (B) word order  
(C) collocation (D) omission

## Computer:

**111.** When the Value of 37H is divided by 17H, the remainder

- (A) COH (B) 03H  
(C) 07H (D) 09H

**112.** The number of Boolean function possible with  $n$  binary variables is equal to

- (A)  $2^{2^n}$  (B)  $2^n$   
(C)  $2^{2^{n+1}}$  (D)  $2^{n+1}$

**113.** Consider 4-bit gray code representation of numbers. Let  $h_3h_2h_1h_0$  be the gray code representation of a number  $n$  and  $g_3g_2g_1g_0$  be the gray code representation of the number  $(n + 1)$  modulo 15. Which one of the following functions is correct?

- (A)  $g_0(h_3h_2h_1h_0) = \sum(1, 2, 3, 6, 10, 13, 14, 15)$   
(B)  $g_1(h_3h_2h_1h_0) = \sum(4, 9, 10, 11, 12, 13, 14, 15)$   
(C)  $g_2(h_3h_2h_1h_0) = \sum(2, 4, 5, 6, 7, 12, 13, 15)$   
(D)  $g_3(h_3h_2h_1h_0) = \sum(0, 1, 6, 7, 10, 11, 12, 13)$

**114.** The minimum number NAND gates required to realize  $AB + AB'C + AB'C'$  is

- (A) 3 (B) 2  
(C) 1 (D) 0

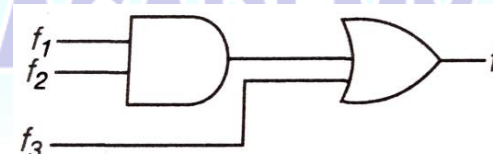
**115.** Which optical phenomenon is utilized in the operation of the latest write-once optical storage medium called digital paper?

- (A) Polarisation (B) Interference  
(C) Internal reflection (D) Diffraction

**116.** P is a 16-bit signed integer. The 2's Complement representation of P is  $(F87B)_{16}$ . The 2's complement representation of  $8P$  is

- (A)  $(C3D8)_{36}$  (B)  $(187B)_{16}$   
(C)  $(188B)_{16}$  (D)  $(987B)_{16}$

**117.** Given,  $f_1, f_3$  and  $f$  is canonical sum of products form (in decimal) from the circuit.



$$f_1 = \sum m(4, 5, 6, 7, 8), f_3 = \sum m(1, 6, 15)$$

and  $f = \sum m(1, 6, 8, 15)$ , then  $f_2$  is

- (A)  $\sum(4, 6)$  (B)  $\sum(4, 8)$   
(C)  $\sum(6, 8)$  (D)  $\sum(4, 6, 8)$





# ACME ACADEMY

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118. Which of the following is equivalent to the expression  $\overline{(X + Y + Z)}$ ?

- (A)  $(\bar{X} + \bar{Y})Z$  (B)  $(X + Y)\bar{Z}$   
(C)  $(\bar{X} + \bar{Y})\bar{Z}$  (D)  $(X + Y)Z$

119.  $\{p \rightarrow q \vee r, q \rightarrow s, r \rightarrow s\}$  is logically equivalent to

- (A)  $q \rightarrow r$  (B)  $r \rightarrow q$   
(C)  $p \rightarrow s$  (D)  $s \rightarrow p$

120. The minimum number of MOS transistors required to make a dynamic RAM cell is

- (A) 1 (B) 2  
(C) 3 (D) 4







# ACME ACADEMY

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## Answer Key

1. C	13. D	25. D	37. B	49. D	61. A	73. C	85. C	97. A	109. A
2. A	14. B	26. B	38. A	50. B	62. B	74. D	86. A	98. D	110. D
3. D	15. D	27. C	39. C	51. A	63. D	75. D	87. B	99. B	111. D
4. A	16. A	28. A	40. A	52. D	64. D	76. D	88. A	100. B	112. B
5. D	17. C	29. D	41. .	53. B	65. A	77. C	89. C	101. B	113. B
6. C	18. B	30. A	42. B	54. B	66. A	78. C	90. A	102. A	114. B
7. C	19. A	31. .	43. D	55. C	67. C	79. D	91. A	103. B	115. D
8. .	20. C	32. C	44. A	56. B	68. C	80. D	92. B	104. A	116. A
9. C	21. C	33. B	45. A	57. B	69. C	81. D	93. B	105. C	117. C
10. .	22. B	34. D	46. D	58. D	70. B	82. A	94. A	106. B	118. D
11. A	23. B	35. A	47. A	59. A	71. B	83. B	95. D	107. C	119. C
12. B	24. B	36. .	48. C	60. A	72. A	84. A	96. C	108. B	120. A

ACME  
MCA  
ENTRANCE ACADEMY



### Solution

1. (\*) None option is correct.

2. (a) We have,  $\tan = \frac{7\pi}{8}$

$$= \tan\left(\pi - \frac{\pi}{8}\right) = -\tan \frac{\pi}{8} = -\left(\frac{1 - \cos \frac{\pi}{4}}{\sin \frac{\pi}{4}}\right)$$

$$\Rightarrow -\tan \frac{\pi}{8} = -\left(\frac{1 - \frac{1}{\sqrt{2}}}{\frac{1}{\sqrt{2}}}\right) = 1 - \sqrt{2}$$

3. (d) We have,  $|a| = 13$ ,  $|b| = 5$ ,  $a \cdot b = 60$

$$|a \times b| = \sqrt{|a|^2 \cdot |b|^2 - (a \cdot b)^2}$$

$$|a \times b| = \sqrt{13^2 \times 5^2 - (60)^2}$$

$$= \sqrt{169 \times 25 - 3600}$$

$$= \sqrt{4425 - 3600} = \sqrt{625} = 25$$

4. (a) Let the height of first tower is PQ.

$$\therefore PQ = AD$$

In given figure

$$\text{In } \triangle APB, \tan 60^\circ = \frac{AB}{PA}$$

$$\Rightarrow \sqrt{3} PA = AB$$

In  $\triangle BQD$ ,

$$\tan 30^\circ = \frac{BD}{QD}$$

$$\frac{1}{\sqrt{3}} = \frac{BD}{QD}$$

$$QD = \sqrt{3}BD$$

$$PA = \sqrt{3}BD$$

$$\Rightarrow PA = \sqrt{3} [AB - AD]$$

From Eq. (i) and (ii), we get

$$PA = \sqrt{3} (\sqrt{3}PA - AD)$$

$$PA = 3PA - \sqrt{3}AD$$

$$\sqrt{3}AD = 2PA$$

$$AD = \frac{2 \times 25}{\sqrt{3}}$$

$$AD = \frac{50}{\sqrt{3}}$$

Hence, height of first tower is  $\frac{50}{\sqrt{3}}$  m.

5. (d) Since,  $a = 4\hat{i} + 6\hat{j}$  and  $b = 3\hat{i} + 4\hat{k}$

Vector component of  $a$  along  $b$  is  $\frac{(a \cdot b)b}{b^2}$

$$= \frac{(4\hat{i} + 6\hat{j}) \cdot (3\hat{i} + 4\hat{k})}{(\sqrt{3^2 + 4^2})^2} (3\hat{i} + 4\hat{k})$$

$$= \frac{36}{25} (3\hat{i} + 4\hat{k})$$

6. (c) We have,  $\sin^{-1} \frac{1}{\sqrt{2}} + \sin^{-1} \frac{\sqrt{2} - \sqrt{1}}{\sqrt{6}} + \sin^{-1} \frac{\sqrt{3} - \sqrt{2}}{\sqrt{12}} + \dots \infty$

$$\Rightarrow \sum_{n=1}^{\infty} \sin^{-1} \left( \frac{\sqrt{x} - \sqrt{x-1}}{\sqrt{x(x+1)}} \right)$$

$$= \sum_{n=1}^{\infty} \tan^{-1} \sqrt{x} - \tan^{-1} \sqrt{x-1}$$

$$\Rightarrow \sum_{n=1}^{\infty} \tan^{-1} \sqrt{x} - \tan^{-1} \sqrt{x-1} = \tan^{-1} \infty = \frac{\pi}{2}$$

7. (c) Given, equation of circles are

$$x^2 + y^2 + 2gx + 2fy = 0 \text{ and } x^2 + y^2 + 2g'x + 2f'y = 0$$

Two circle touch each other

$\therefore$  Distance between centre of circle = Sum of radius of two circles

i.e.  $C_1C_2 = r_1 + r_2$  [ $\because C_1$  and  $C_2$  are centre of circle]

$$\Rightarrow \sqrt{(g-g')^2 + (f-f')^2} = \sqrt{(g^2 + f^2)} + \sqrt{(g'^2 + f'^2)}$$

Squaring on both sides,

$$g^2 + g'^2 - 2gg' + f^2 + f'^2 - 2ff' = g^2 + f^2 + g'^2 + f'^2 + 2\sqrt{(g^2 + f^2)(g'^2 + f'^2)}$$

$$\Rightarrow -(gg' + ff') = \sqrt{(g^2 + f^2)(g'^2 + f'^2)}$$

Again squaring, we get

$$g^2g'^2 + f^2f'^2 + 2gg'ff' = g^2g'^2 + g^2f'^2 + g'^2f^2 + f^2f'^2$$

$$\Rightarrow g^2g'^2 + f^2f'^2 - 2gg'ff' + f' = 0$$

$$\Rightarrow (gg' - ff')^2 = 0 \Rightarrow gg' = ff'$$

9. (c) Let ABC is a right angle triangle and  $\angle B = 90^\circ$ .

We have,  $AC = 4AD$ .

Let

$$BD = x$$

$$\therefore AC = 4x$$

$$\angle BDC = 90^\circ$$

In  $\triangle BDC$ ,

$$\sin \theta = \frac{BD}{BC}$$

$$\Rightarrow BC = \frac{x}{\sin \theta}$$

In  $\triangle ABC$ ,

$$\cos \theta = \frac{BC}{AC}$$

$$\Rightarrow \cos \theta = \frac{BC}{4x}$$

$$\Rightarrow BC = 4x \cos \theta \quad \dots (ii)$$

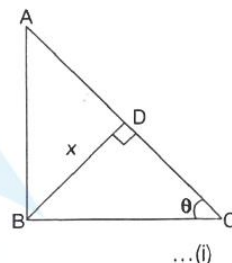
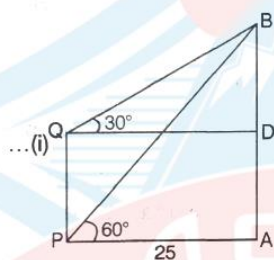
From Eqs. (i) and (ii) we get

$$4x \cos \theta = \frac{x}{\sin \theta}$$

$$2 \sin \theta \cos \theta = \frac{1}{2}$$

$$\Rightarrow \sin 2\theta = \frac{1}{2}$$

$$\Rightarrow 2\theta = 30^\circ \Rightarrow \theta = 15^\circ$$



11. (a) Angles of a triangle are in the ratio 2 : 3 : 7

$$\therefore 2x + 3x + 7x = 180^\circ$$

$$\Rightarrow x = 15^\circ$$

Since, angles of triangle are  $30^\circ, 45^\circ, 105^\circ$

$$\therefore \frac{a}{\sin 30^\circ} = \frac{b}{\sin 45^\circ} = \frac{c}{\sin 105^\circ}$$

$$\Rightarrow \frac{a}{1/2} = \frac{b}{1/\sqrt{2}} = \frac{c}{\frac{\sqrt{3}+1}{2\sqrt{2}}}$$

$$\therefore a : b : c = \sqrt{2} : 2 : \sqrt{3} + 1$$

12. (b) We have,  $P(A) = \frac{1}{2}$  and  $P(B) = \frac{1}{3}$

Now,  $P(A) > P(B)$

$$\therefore P(A \cap B) \leq P(B)$$

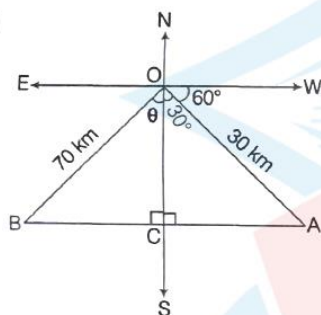
$$\Rightarrow P(A \cap B) \leq \frac{1}{3}$$

13. (d) Let  $A = \{1, 2, 3\}$  and  $B = \{1, 2, 3, 4, 5\}$

$\therefore$  Number of one-to-one function is

$${}^5P_3 = \frac{5!}{2!} = 60$$

14. (b)



In  $\triangle OAC$ ,

$$\sin 30^\circ = \frac{AC}{OA}$$

$$\Rightarrow \frac{1}{2} = \frac{AC}{30}$$

$$\Rightarrow AC = 15 \text{ km}$$

$$\text{Also, } \cos 30^\circ = \frac{OC}{OA}$$

$$= \frac{\sqrt{3}}{2} = \frac{OC}{30}$$

$$\Rightarrow OC = 15\sqrt{3}$$

In  $\triangle OBC$ ,

$$\cos \theta = \frac{OC}{OB} = \frac{15\sqrt{3}}{70}$$

Also, In  $\triangle OBC$ ,

$$\sin \theta = \frac{BC}{OB}$$

$$\Rightarrow \sin \theta = \frac{BC}{70}$$

$$\Rightarrow 1 - \cos^2 \theta = \frac{BC^2}{4900}$$

$$\Rightarrow 1 - \frac{(15\sqrt{3})^2}{4900} = \frac{BC^2}{4900}$$

$$\Rightarrow BC^2 = 4225$$

$$\Rightarrow BC = 65$$

$$\therefore \text{Total distance travelled} = AC + BC = 15 + 65 = 80$$

The time at which ship will cover 70 km from the fort

$$= \frac{80}{10} = 8 \text{ h} \quad [\because \text{Speed of ship} = 10 \text{ km/h}]$$

$\therefore$  The ship will reach at 8 pm.

15. (d) Since,  $x, y$  and  $z$  are three consecutive positive numbers.

$$\therefore x = y - 1 \text{ and } z = y + 1$$

$$\text{Now, } \log(1 + xz) = \log[1 + (y - 1)(y + 1)]$$

$$\log = (1 + y^2 - 1)$$

$$= \log y^2 = 2 \log y$$

16. (a) Since,  $a, b$  and  $c$  are in GP.

$\therefore ax, bx$  and  $cx$  will also in GP.

and  $\log ax, \log bx$  and  $\log cx$  are in AP.

$[\because a, b, c$  are in AP, then  $\log a$  and  $\log b$  and  $\log c$  are in AP]

Hence,  $\log_{ax} x, \log_{bx} x$  and  $\log_{cx} x$  are in AP.

17. (c) We have,

$$\vec{a} = \frac{\hat{i} - 2\hat{j}}{\sqrt{5}} \text{ and } \vec{b} = \frac{2\hat{i} + \hat{j} + 3\hat{k}}{\sqrt{14}}$$

$$(2\vec{a} + \vec{b}) \cdot [(\vec{a} \times \vec{b}) \times (\vec{a} - 2\vec{b})]$$

$$\Rightarrow (2\vec{a} + \vec{b}) \cdot [\vec{a} \cdot (\vec{a} - 2\vec{b})\vec{b} - (\vec{a} - 2\vec{b})\vec{a}]$$

$$[\because (\vec{a} \times \vec{b}) \times \vec{c} = (\vec{a} \cdot \vec{c})\vec{b} - (\vec{b} \cdot \vec{c})\vec{a}]$$

$$\Rightarrow (2\vec{a} + \vec{b}) \cdot [(\vec{a}^2 - 2\vec{a} \cdot \vec{b})\vec{b} - (\vec{b} \cdot \vec{a} - 2\vec{b}^2)\vec{a}]$$

$$\Rightarrow [2\vec{a} + \vec{b}] \cdot [(1 - 0)\vec{b} - (1 - 2)\vec{a}]$$

$$[\because \vec{a}^2 = 1 = \vec{b}^2, \vec{a} \cdot \vec{b} = 0]$$

$$[2\vec{a} + \vec{b}] \cdot [\vec{b} + 2\vec{a}]$$

$$\Rightarrow 4\vec{a}^2 + 4\vec{a} \cdot \vec{b} + \vec{b}^2$$

$$\Rightarrow 4 + 0 + 1 = 5$$

18. (b) We have,

$$\frac{1}{2\sqrt{1} + 1\sqrt{2}} + \frac{1}{3\sqrt{2} + 2\sqrt{3}} + \frac{1}{4\sqrt{3} + 3\sqrt{4}} \dots + \frac{1}{25\sqrt{24} + 24\sqrt{25}}$$

Now,

$$T_n = \frac{1}{(n+1)\sqrt{n} + n\sqrt{n+1}}$$

$$\Rightarrow T_n = \frac{1}{\sqrt{n}\sqrt{n+1} + 1(\sqrt{n+1} + \sqrt{n})}$$

$$\Rightarrow T_n = \frac{\sqrt{n+1} - \sqrt{n}}{\sqrt{n}\sqrt{n+1} + 1} = \frac{1}{\sqrt{n}} - \frac{1}{\sqrt{n+1}}$$

$$S = \frac{1}{\sqrt{1}} - \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} - \frac{1}{\sqrt{3}} \dots - \frac{1}{\sqrt{24}} + \frac{1}{\sqrt{25}}$$

$$= 1 - \frac{1}{\sqrt{25}} = 1 - \frac{1}{5} = \frac{4}{5}$$



19. (a) We have,  $\mathbf{a} = \hat{i} - \hat{k}$ ,  $\mathbf{b} = x\hat{i} + \hat{j} + (1-x)\hat{k}$   
and  $\mathbf{c} = y\hat{i} + \hat{j} + (1+x-y)\hat{k}$

Now,

$$[\mathbf{a}\mathbf{b}\mathbf{c}] = \begin{vmatrix} 1 & 0 & -1 \\ x & 1 & 1-x \\ y & x & 1+x-y \end{vmatrix}$$

$$c_1 \rightarrow c_1 + c_2 = \begin{vmatrix} 0 & 0 & -1 \\ 1 & 1 & 1-x \\ 1+x & x & 1+x-y \end{vmatrix}$$

Expand along  $R_1$ ,

$$-1[x-1+x] = 1$$

$\therefore$  Neither depends on  $x$  nor on  $y$ .

20. (c) We have,  ${}^{42}P_2 = {}^nP_4$

$$\Rightarrow 42 \frac{n!}{(n-2)!} = \frac{n!}{(n-4)!}$$

$$\Rightarrow \frac{(n-2)!}{(n-4)!} = 42$$

$$\Rightarrow \frac{(n-2)(n-3)(n-4)!}{(n-4)!} = 42$$

$$\Rightarrow n^2 - 5n + 6 = 42$$

$$n^2 - 5n - 36$$

$$\Rightarrow (n-9)(n+4) = 0$$

$$n = 9$$

21. (a)  $(\mathbf{a} \times \mathbf{b}) \cdot \mathbf{a} = [\mathbf{a}, \mathbf{b}, \mathbf{a}] = 0$

$$(b) (\mathbf{a} + \mathbf{b}) \cdot (\mathbf{a} \times \mathbf{b}) = [\mathbf{a}, \mathbf{a}, \mathbf{b}] + [\mathbf{b}, \mathbf{a}, \mathbf{b}] = 0 + 0 = 0$$

$$(c) (\mathbf{a} + \mathbf{b}) \cdot (\mathbf{a} - \mathbf{b}) = |\mathbf{a}|^2 - |\mathbf{b}|^2 \neq 0$$

$$(d) (\mathbf{a} - \mathbf{b}) \cdot (\mathbf{a} \times \mathbf{b}) = [\mathbf{a}, \mathbf{a}, \mathbf{b}] - [\mathbf{b}, \mathbf{a}, \mathbf{b}] = 0 - 0 = 0$$

Hence, option (c) is correct.

22. (b) We have,

$$A = \begin{bmatrix} a & b & c \\ b & c & a \\ c & a & b \end{bmatrix}$$

It is given that,  $abc = 1$  and  $A^T A = I$

$$A^T A = \begin{bmatrix} a & b & c \\ b & c & a \\ c & a & b \end{bmatrix} \begin{bmatrix} a & b & c \\ b & c & a \\ c & a & b \end{bmatrix}$$

$$\begin{bmatrix} a^2 + b^2 + c^2 & ab + bc + ca & ac + ab + bc \\ ab + bc + ca & b^2 + c^2 + a^2 & ab + bc + ca \\ ab + bc + ca & ab + bc + ca & c^2 + a^2 + b^2 \end{bmatrix}$$

Now,  $A^T A = I$

$$\begin{bmatrix} a^2 + b^2 + c^2 & ab + bc + ca & ab + bc + ca \\ ab + bc + ca & a^2 + b^2 + c^2 & ab + bc + ca \\ ab + bc + ca & ab + bc + ca & a^2 + b^2 + c^2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\therefore a^2 + b^2 + c^2 = 1$$

but  $ab + bc + ca \neq 0$  [ $\because a, b, c$  are real positive numbers]

$$\text{Hence, } a^2 + b^2 + c^2 = 1$$

23. (b) We have,  $x = a \cos 2t$  and  $y = 2\sqrt{2} a \sin t$

$$\frac{dx}{dt} = -2a \sin 2t \text{ and } \frac{dy}{dt} = 2\sqrt{2} a \cos t$$

$$\therefore \frac{dy}{dx} = \frac{2\sqrt{2} a \cos t}{-2a \sin 2t}$$

$$= \frac{-\sqrt{2} \cos t}{\sin^2 t}$$

$$\Rightarrow \frac{dy}{dx} = \frac{-\sqrt{2} \cos t}{2 \sin t \cos t} = \frac{-1}{\sqrt{2} \sin t}$$

It is given that,  $m$  is the slope of tangent.

$$\therefore m = -\frac{1}{\sqrt{2} \sin t}$$

$$\Rightarrow \sqrt{2} \sin t = \frac{-1}{m}$$

Squaring both sides,

$$\Rightarrow 2 \sin^2 t = \frac{1}{m^2}$$

$$\Rightarrow 1 - \cos 2t = \frac{1}{m^2}$$

$$\Rightarrow 1 - \frac{1}{m^2} = \cos 2t$$

$$\Rightarrow \frac{m^2 - 1}{m^2} = \cos 2t$$

Equation of tangent of curve is

$$y - 2\sqrt{2} a \sin t = m(x - a \cos 2t)$$

$$y - 2a \left( \frac{-1}{m} \right) = m \left( x - a \left( \frac{m^2 - 1}{m^2} \right) \right)$$

$$\Rightarrow y = mx - ma \left( \frac{m^2 - 1}{m^2} \right) - \frac{2a}{m}$$

$$\Rightarrow y = mx - a \left( \frac{m^2 - 1 + 2}{m} \right)$$

$$\Rightarrow y = mx - a \left( m + \frac{1}{m} \right)$$

24. (b) Let  $(h, k)$  be the mid-point of chord of parabola  $y^2 = 4x$ .

$$\therefore \text{Equation of chord is } yk - 2(x + h) = k^2 - 4h$$

$$[\because \text{Equation of chord of parabola when mid-point } (x, y) \text{ is } T = S_1]$$

$$\Rightarrow yk - 2x - 2h = k^2 - 4h \quad \dots (i)$$

Chord are drawn through vertex

$$\therefore h = \frac{x}{2} \text{ and } k = \frac{y}{2}$$

$$\Rightarrow 2h = x \text{ and } 2k = y$$

Putting the values of  $x$  and  $y$  in Eq. (i), we get

$$2k^2 - 4h - 2h = k^2 - 4h \quad k^2 = 2h$$

$\therefore$  Locus of the mid-point of the parabola is  $y^2 = 2x$ .

25. (d) We have,  $\lim_{x \rightarrow a} \frac{\sqrt{a+2x} - \sqrt{3x}}{\sqrt{3a+x} - 2\sqrt{x}}$

$$\begin{aligned} &\Rightarrow \lim_{x \rightarrow a} \frac{(\sqrt{a+2x} - \sqrt{3x})(\sqrt{a+2x} + \sqrt{3x})(\sqrt{3a+x} + 2\sqrt{x})}{(\sqrt{3a+x} - 2\sqrt{x})(\sqrt{a+2x} + \sqrt{3x})(\sqrt{3a+x} + 2\sqrt{x})} \\ &\Rightarrow \lim_{x \rightarrow a} \frac{(a+2x-3x)(\sqrt{3a+x} + 2\sqrt{x})}{(3a+x-4x)(\sqrt{a+2x} + \sqrt{3x})} \\ &\Rightarrow \lim_{x \rightarrow a} \frac{(a-x)(\sqrt{3a+x} + 2\sqrt{x})}{3(a-x)(\sqrt{a+2x} + \sqrt{3x})} \\ &\Rightarrow \frac{1}{3} \times \frac{4}{2\sqrt{3}} = \frac{2}{3\sqrt{3}} \end{aligned}$$

26. (b) We have,  $\int_{-\pi/3}^{\pi/3} \frac{x \sin x}{\cos^2 x} dx$

$$\begin{aligned} \text{Let } I &= \int_{-\pi/3}^{\pi/3} \frac{x \sin x}{\cos^2 x} dx \\ &\Rightarrow I = 2 \int_0^{\pi/3} \frac{x \sin x}{\cos^2 x} dx \quad \left[ \because \frac{x \sin x}{\cos^2 x} \text{ is an even function} \right] \\ &\Rightarrow I = 2 \int_0^{\pi/3} x \sec x \tan x dx \\ &\Rightarrow I = 2 \left[ x \int \sec x \tan x dx - \int \frac{dx}{dx} \int \sec x \tan x dx \cdot dx \right]_0^{\pi/3} \\ &\Rightarrow I = 2 \left[ [x \sec x]_0^{\pi/3} - [\log(\sec x + \tan x)]_0^{\pi/3} \right] \\ &\Rightarrow I = 2 \left[ \frac{\pi}{3} \sec \frac{\pi}{3} - \log \left( \sec \frac{\pi}{3} + \tan \frac{\pi}{3} \right) \right] \\ &\Rightarrow I = \frac{4\pi}{3} - 2 \log \left[ \frac{1 + \sin \frac{\pi}{3}}{\cos \frac{\pi}{3}} \right] \\ &\Rightarrow I = \frac{4\pi}{3} - 2 \log \left[ \frac{\left( \cos \frac{\pi}{6} + \sin \frac{\pi}{6} \right)^2}{\cos^2 \frac{\pi}{6} - \sin^2 \frac{\pi}{6}} \right] \\ &\Rightarrow I = \frac{4\pi}{3} - 2 \log \left[ \frac{\cos \frac{\pi}{6} + \sin \frac{\pi}{6}}{\cos \frac{\pi}{6} - \sin \frac{\pi}{6}} \right] \\ &\Rightarrow I = \frac{4\pi}{3} - 2 \log \tan \left( \frac{\pi}{4} + \frac{\pi}{6} \right) \\ &\Rightarrow I = \frac{4\pi}{3} - 2 \log \tan \frac{5\pi}{12} \end{aligned}$$

27. (c) The foci of the ellipse  $\frac{x^2}{16} + \frac{y^2}{b^2} = 1$

and the hyperbola  $\frac{x^2}{144} - \frac{y^2}{81} = \frac{1}{25}$  coincide

$\therefore$  Foci of the ellipse and hyperbola lie on X-axis.

Foci of the ellipse =  $\sqrt{16 - b^2}$

and foci of the hyperbola =  $\sqrt{\frac{144}{25} + \frac{81}{25}}$

Foci of the ellipse and hyperbola coincide

$$\therefore \sqrt{16 - b^2} = \sqrt{\frac{144}{25} + \frac{81}{25}}$$

Squaring both sides,

$$\Rightarrow 16 - b^2 = \frac{225}{25}$$

$$\Rightarrow b^2 = 16 - 9 = 7$$

28. (a) We have,

$$\text{Let } A = \begin{bmatrix} \sin(A+B+C) & \sin B & \cos C \\ -\sin B & 0 & \tan A \\ \cos(A+B) & -\tan A & 0 \end{bmatrix}$$

$$\Rightarrow A = \begin{bmatrix} \sin \pi & \sin B & \cos C \\ -\sin B & 0 & \tan A \\ \cos(\pi - C) & \tan A & 0 \end{bmatrix} \quad [\because A+B+C = \pi]$$

$$\Rightarrow A = \begin{bmatrix} 0 & \sin B & \cos C \\ -\sin B & 0 & \tan A \\ -\cos C & \tan A & 0 \end{bmatrix}$$

$$A = 0 \quad [\because A \text{ is skew-symmetric}]$$

$$|A| = 0 \text{ Matrix}$$

29. (d) Mean =  $\frac{1+1+d+1+2d+\dots+1+100d}{101}$

$$\text{Mean} = \frac{101+d(1+2+3+\dots+100)}{101}$$

$$\Rightarrow \text{Mean} = \frac{101+d \left( \frac{100 \times 101}{2} \right)}{101} = \frac{101(1+50d)}{101} = 50d+1$$

$$\Rightarrow \text{MD}(\bar{x}) = \frac{\sum |x_i - \bar{x}|}{n}$$

$$= \frac{|1-50d-1| + |1+d-50d-1| + \dots + |1+100d-50d-1|}{101}$$

$$\Rightarrow 225 = \frac{(50d+49d+\dots+d) + (d+2d+3d+\dots+50d)}{101}$$

$$\Rightarrow 225 = \frac{2d(1+2+3+\dots+50)}{101}$$

$$\Rightarrow 225 = \frac{2d(50 \times 51)}{2 \times 101} \Rightarrow d = \frac{225 \times 101}{50 \times 51} = 891$$

None option is correct.

30. (a) We have, equation of line is  $x+y=1$  ... (i)

A line perpendicular to the given line is  $-x+y=\lambda$

This line is passing through (2, 4).

$$\therefore -2+4=\lambda$$

$$\Rightarrow \lambda=2$$

Hence, equation of line is  $-x+y=2$  ... (ii)

Solving Eqs. (i) and (ii), we get

$$x = \frac{-1}{2} \text{ and } y = \frac{3}{2}$$

$\therefore$  foot of perpendicular is  $\left( \frac{-1}{2}, \frac{3}{2} \right)$



32. (c) We have  $(k-2)x^2 + 8x + k + 4 = 0$  has both real, distinct and negative and negative roots.

There are three cases

(i)  $D > 0$

(ii) Sum of roots  $< 0$  i.e.  $-\frac{b}{a} < 0$

(iii) Product of roots  $> 0$  i.e.  $\frac{c}{a} > 0$

Case I  $D > 0$

$$64 - 4(k-2)(k+4) > 0$$

$$16 - (k^2 + 2k - 8) > 0$$

$$\Rightarrow k^2 + 2k - 24 < 0$$

$$(k+6)(k-4) < 0$$

$$-6 < k < 4$$

... (i)

Case II Sum of roots  $< 0$

$$\therefore \frac{-8}{k-2} < 0$$

$$\Rightarrow \frac{8}{k-2} > 0$$

$$\Rightarrow k > 2$$

... (ii)

Case III Product of roots  $> 0$

$$\therefore \frac{k+4}{k-2} > 0$$

$$\therefore K \in (-\infty, -4) \cup (2, \infty)$$

... (iii)

From Eqs. (i), (ii) and (iii) We get

$k = 3$  is satisfied

Hence, value of  $k = 3$

33. (b) Let  $D, E$  and  $F$  are the mid-points of the sides  $BC, CA$  and  $AB$  of  $\triangle ABC$ .

$BC$  is parallel to side  $EF$  and passes through  $(2, 1)$ .

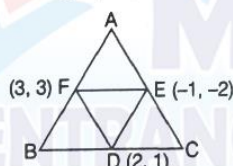
$\therefore$  Equation of line  $BC$  is

$$y - 1 = \frac{3+2}{3+1}(x - 2)$$

$$\Rightarrow y - 1 = \frac{5}{4}(x - 2)$$

$$\Rightarrow 4y - 4 = 5x - 10$$

$$\Rightarrow 5x - 4y - 6 = 0$$



34. (d) Let  $A$  be the event 1 appear on the die

$$\therefore P(A) = \frac{1}{6}, P(\bar{A}) = 1 - \frac{1}{6} = \frac{5}{6}$$

Now, 1 appears in an even numbered throw.

Required probability

$$= P(\bar{A}) \cdot P(A) + P(\bar{A}) \cdot P(\bar{A}) \cdot P(A) + \dots$$

$$= \frac{5}{6} \times \frac{1}{6} + \frac{5}{6} \times \frac{5}{6} \times \frac{1}{6} + \dots$$

$$= \frac{5}{6} \times \frac{1}{6} \left[ 1 + \frac{25}{36} + \left( \frac{25}{36} \right)^2 + \dots \right] = \frac{5}{36} \left( \frac{1}{1 - \frac{25}{36}} \right) = \frac{5}{11}$$

35. (a) We have,

$$\mathbf{a} = \hat{i} + \hat{j} + \mathbf{k},$$

$$\mathbf{b} = \hat{i} - \hat{j} + \mathbf{k} \text{ and}$$

$$\mathbf{c} = \hat{i} - \hat{j} - \mathbf{k}$$

A vector  $\mathbf{v}$  in plane of  $\mathbf{a}$  and  $\mathbf{b}$

$$\therefore \mathbf{v} = \lambda \mathbf{a} + \mu \mathbf{b}$$

$$\Rightarrow = \lambda(\hat{i} + \hat{j} + \mathbf{k}) + \mu(\hat{i} - \hat{j} + \mathbf{k})$$

$$= (\lambda + \mu)\hat{i} + (\lambda - \mu)\hat{j} + (\lambda + \mu)\mathbf{k}$$

Projection of  $\mathbf{v}$  and  $\frac{\mathbf{c}}{|\mathbf{c}|}$  is  $\frac{1}{\sqrt{3}}$

$$\therefore \frac{(\lambda + \mu)\hat{i} + (\lambda - \mu)\hat{j} + (\lambda + \mu)\mathbf{k} \cdot (\hat{i} - \hat{j} - \mathbf{k}) / \sqrt{3}}{\left| \frac{\mathbf{c}}{|\mathbf{c}|} \right|} = \frac{1}{\sqrt{3}}$$

$$\frac{(\lambda + \mu) - (\lambda - \mu) - (\lambda + \mu)}{\sqrt{3}} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow \lambda - \mu = -1$$

$\therefore$  Option (a) is correct.

37. (b) We have,  $0 < x < \pi$  and

$$\cos x + \sin x = \frac{1}{2}$$

$$\Rightarrow (\cos x + \sin x)^2 = \frac{1}{4}$$

$$\Rightarrow 1 + \sin 2x = \frac{1}{4}$$

$$\Rightarrow \sin 2x = \frac{-3}{4}$$

$$\Rightarrow \frac{2 \tan x}{1 + \tan^2 x} = \frac{-3}{4}$$

$$\Rightarrow 3 \tan^2 x + 8 \tan x + 3 = 0$$

$$\tan x = \frac{-8 \pm \sqrt{64 - 36}}{6}$$

$$\tan x = \frac{-8 \pm 2\sqrt{7}}{6} = \frac{-4 \pm \sqrt{7}}{3}$$

$$\tan x = \frac{-(4 + \sqrt{7})}{3}$$

$$\frac{-4 + \sqrt{7}}{3}$$

or

38. (a) We have  $\mathbf{a}, \mathbf{b}$  and  $\mathbf{c}$  are the position vectors of the vertices of  $\triangle ABC$ .

$$\text{Area of triangle } ABC = \frac{1}{2} |\mathbf{AB} \times \mathbf{AC}|$$

$$= \frac{1}{2} |(\mathbf{b} - \mathbf{a}) \times (\mathbf{c} - \mathbf{a})|$$

$$= \frac{1}{2} |(\mathbf{b} \times \mathbf{c}) + (\mathbf{a} \times \mathbf{b}) + (\mathbf{c} \times \mathbf{a}) + \mathbf{a} \times \mathbf{a}|$$

$$= \frac{1}{2} |(\mathbf{a} \times \mathbf{b}) + \mathbf{b} \times \mathbf{c} + \mathbf{c} \times \mathbf{a}|$$

$$[\because \mathbf{a} \times \mathbf{a} = 0]$$



39. (c) We have,

$$\int e^x [f(x) - f'(x)] dx = \phi x$$

$$\Rightarrow \int e^x [f(x) dx - \int e^x f'(x) dx] = \phi x$$

$$\Rightarrow \int e^x f(x) dx - \left[ e^x \int f'(x) dx - \int \frac{de^x}{dx} \int f(x) dx \cdot dx \right] = \phi x$$

$$\Rightarrow \int e^x f(x) dx - [e^x f(x) - \int e^x f'(x) dx] = \phi x$$

$$\Rightarrow \int e^x f(x) dx - e^x f(x) + \int e^x f'(x) dx = \phi x$$

$$\Rightarrow 2 \int e^x f(x) dx = \phi x + e^x f(x)$$

$$\Rightarrow \int e^x f(x) dx = \frac{1}{2} [\phi x + e^x f(x)]$$

40. (a) We have,  $3x + 4y + k = 0$  is tangent of the hyperbola

$$9x^2 - 16y^2 = 144$$

$$\text{Equation of hyperbola is } 9x^2 - 16y^2 = 144$$

$$\Rightarrow \frac{x^2}{16} - \frac{y^2}{9} = 1$$

$$\text{Equation of tangent is } 3x + 4y + k = 0$$

We know that,  $y = mx + c$  touches the hyperbola.

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \text{ if } c^2 = a^2 m^2 - b^2$$

$$\therefore \left( \frac{-k}{4} \right)^2 = 16 \left( \frac{-3}{4} \right)^2 - 9$$

$$\Rightarrow \frac{k^2}{16} = 9 - 9$$

$$\Rightarrow k = 0$$

42. (b) We have,  $(-4, 5)$  is one vertex of the square and equation of diagonal is  $7x - y + 8 = 0$ . Diagonals of square are perpendicular to each other.

$\therefore$  Equation of other diagonal which is perpendicular to

$$7x - y + 8 = 0 \text{ is}$$

$$x + 7y = \lambda$$

It passes through  $(-4, 5)$

$$\therefore -4 + 35 = \lambda \Rightarrow \lambda = 31$$

Hence, equation of diagonal is,  $x + 7y = 31$ .

43. (d) We have,

$$\text{Total number of tickets} = (2n + 1)$$

Total number of outcomes of 3 numbers are drawn from  $(2n + 1)$  tickets is  ${}^{2n+1}C_3$

$$= \frac{(2n+1)}{3! (2n-2)!} = \frac{(2n+1)(2n)(2n-1)}{3!}$$

$$= \frac{n(4n^2 - 1)}{3}$$

Favourable outcomes are if three numbers are in AP

$$(2n - 1 + 2n - 3 + 2n - 5 \dots + 5 + 3 + 1) = n^2$$

$$\therefore \text{Required probability} = \frac{\frac{n^2}{n(4n^2 - 1)}}{\frac{n(4n^2 - 1)}{3}} = \frac{3n}{4n^2 - 1}$$

44. (a) Let the centre of circle is  $(h, k)$  and radius of circle is  $k$ .

Centre of another circle  $(0, 3)$  and radius is 2.

Both circles touch each other.

$$\therefore \sqrt{(h-0)^2 + (k-3)^2} = k + 2$$

$$\Rightarrow \sqrt{h^2 + k^2 - 6k + 9} = k + 2$$

$$\Rightarrow h^2 + k^2 - 6k + 9 = k^2 + 4k + 4$$

$$\Rightarrow h^2 = 10k - 5$$

$$\Rightarrow x^2 = 10y - 5 \text{ which represent equation of parabola.}$$

$\therefore$  Locus of centre of circle is parabola.

45. (a) We have,

$$(P - Q) \cup (Q - P) \cup (P \cap Q)$$

$$\Rightarrow (P \cap Q') \cup (Q \cap P') \cup (P \cap Q)$$

$$\Rightarrow (P \cap Q') \cup [(Q \cap P') \cup (Q \cap P)]$$

$$\Rightarrow (P \cap Q') \cup [Q \cap (P \cup P')]$$

$$\Rightarrow (P \cap Q') \cup (Q \cap U)$$

$$\Rightarrow (P \cap Q') \cup Q$$

$$\Rightarrow (P \cup Q) \cap (Q \cup Q')$$

$$\Rightarrow (P \cup Q) \cap U = (P \cup Q)$$

46. (d) Since,  $\frac{dx}{dy} = \frac{1}{\frac{dy}{dx}} = \left( \frac{dy}{dx} \right)^{-1}$

$$\Rightarrow \frac{d}{dy} \left( \frac{dx}{dy} \right) = \frac{d}{dx} \left( \frac{dy}{dx} \right)^{-1} \frac{dy}{dx}$$

$$\Rightarrow \frac{d^2 x}{dy^2} = - \left( \frac{d^2 y}{dx^2} \right) \left( \frac{dy}{dx} \right)^{-2} \left( \frac{dy}{dx} \right)$$

$$\Rightarrow \frac{d^2 x}{dy^2} = - \left( \frac{d^2 y}{dx^2} \right) \left( \frac{dy}{dx} \right)^{-3}$$

47. (a) We have,

$$\text{Equation of ellipse is } \frac{x^2}{16} + \frac{y^2}{9} = 1$$

$$\text{Here, } a^2 = 16$$

$$\text{and } b^2 = 9$$

We know that, foci of ellipse of

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 \text{ is } (\pm ae, 0)$$

$$ae = \sqrt{a^2 - b^2}$$

$$= \sqrt{16 - 9}$$

$$= \sqrt{7}$$

$\therefore$  Foci of ellipse  $(\pm \sqrt{7}, 0)$ .

It is given that, centre of circle is  $(0, 3)$  and passes through  $\pm \sqrt{7}, 0$

$$\therefore r = \sqrt{(0 + \sqrt{7})^2 + (3 - 0)^2}$$

$$= \sqrt{7 + 9}$$

$$= 4$$

Hence, radius of circle = 4 units

48. (c) We have,

$$f(x) = 2 \sin x + \cos 2x$$

$$f'(x) = 2 \cos x - 2 \sin 2x$$

$$f''(x) = -2 \sin x - 4 \cos 2x$$

For maxima or minima,

$$f'(x) = 0$$

$$\Rightarrow 2 \cos x - 2 \sin 2x = 0$$

$$\Rightarrow \cos x - 2 \sin x \cos x = 0$$

$$\Rightarrow \cos x (1 - 2 \sin x) = 0$$

$$\cos x = 0 \text{ or } 1 - 2 \sin x = 0$$

$$x = \frac{\pi}{2} \text{ or } x = \frac{\pi}{6}, \frac{5\pi}{6}$$

Now,

$$f''\left(\frac{\pi}{2}\right) = -2 \sin \frac{\pi}{2} - 4 \cos \left(\frac{2\pi}{2}\right)$$

$$= -2 + 4 = 2 > 0$$

$$f''\left(\frac{\pi}{6}\right) = -2 \sin \frac{\pi}{6} - 4 \cos \left(\frac{2\pi}{6}\right)$$

$$= -1 - 2 = -3 < 0$$

$$f''\left(\frac{5\pi}{6}\right) = -2 \sin \frac{5\pi}{6} - 4 \cos \left(\frac{10\pi}{6}\right)$$

$$= -1 - 2 = -3 < 0$$

Hence,  $f(x)$  is minimum at  $\frac{\pi}{2}$  and maximum at  $\frac{\pi}{6}$ .

$\therefore f(x)$  has both local minimum and local maximum.

49. (d) We have,

$$M_r = \begin{bmatrix} r & r-1 \\ r-1 & r \end{bmatrix}, r \in N$$

$$|M_r| = r^2 - (r-1)^2$$

$$= r^2 - r^2 + 2r - 1 = 2r - 1$$

Now,

$$|M_1| + |M_2| + |M_3| + \dots + |M_{2015}|$$

$$\Rightarrow 1 + 3 + 5 + 7 + \dots + 3029$$

$$= (2015)^2$$

$$\left[ \because \sum_{n=1}^n (2n-1) = n^2 \right]$$

50. (b) We have,

$$\mathbf{AC} = 2\hat{i} + \hat{j} + \hat{k}$$

$$\mathbf{BD} = -\hat{i} + 3\hat{j} + 2\hat{k}$$

$$\text{Area of quadrilateral } ABCD = |\mathbf{AC} \times \mathbf{BD}|$$

$$\mathbf{AC} \times \mathbf{BD} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 1 & 1 \\ -1 & 3 & 2 \end{vmatrix}$$

$$= (2-3)\hat{i} - (4+1)\hat{j} + (6+1)\hat{k}$$

$$= -\hat{i} - 5\hat{j} + 7\hat{k}$$

$$|\mathbf{AC} \times \mathbf{BD}| = \sqrt{1+25+49}$$

$$= \sqrt{75} = 5\sqrt{3}$$

Solutions [Q. Nos. 51 to 54]

The given information can be represented as:

Stage	Farmer	Starting point of the stage	Ending point of the stage
First	$F_3$	$P_2$	$P_5$
Second	$F_1$	$P_5$	$P_3$
Third	$F_2$	$P_3$	$P_1$
Fourth	$F_4$	$P_1$	$P_4$
Fifth	$F_5$	$P_4$	$P_2$

51. (a) P is the finishing point of .

52. (d) 5th stage is ploughed by .

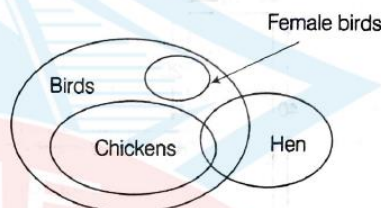
53. (b) P and P

54. (b) P is the starting point of stage 3.

55. (c) The 4th day is Tuesday, then 11th, 12th and 25th also Tuesdays.

Tr days after 24th is 27th, which is Thursday.

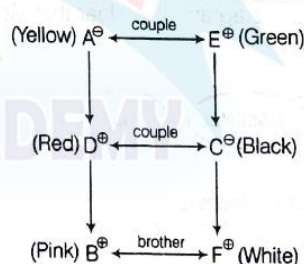
56. (b)



So, only conclusion II and III follow.

Solutions [Q. Nos. 57 to 60]

From the given information, we can draw a relation diagram,



57. (b) A likes yellow colour.

58. (d) Yellow-Hypen green is the colour combination of AE.

59. (a) CD is the married couple.

60. (a) F is the brother of B.

61. (a) As,

E	X	A	M	I	N	A	T	I	O	N
↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓
5	6	1	4	9	5	1	2	9	6	5





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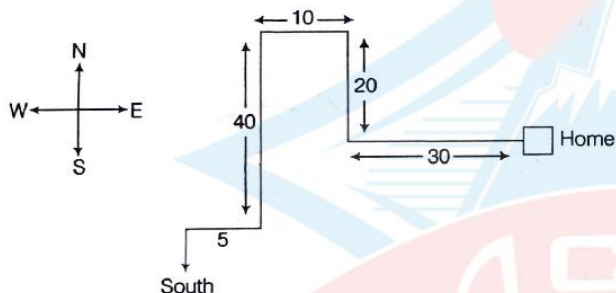
The pattern in the above word is as follows.

$$\begin{aligned} E &= 5 \\ X &= 24 = 2 + 4 = 6 \\ A &= 1 \\ M &= 13 = 1 + 3 = 4 \\ I &= 9 \\ N &= 14 = 1 + 4 = 5 \\ A &= 1 \\ T &= 20 = 2 + 0 = 2 \\ I &= 9 \\ O &= 15 = 1 + 5 = 6 \\ N &= 14 = 1 + 4 = 5 \end{aligned}$$

∴ The sum of the placing value of the words will be the code of the words. Similarly,

$$\begin{array}{cccccccc} G & O & V & E & R & N & M & E & N & T \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 7 & 6 & 4 & 5 & 9 & 5 & 4 & 5 & 5 & 2 \end{array}$$

62. (b) According to the information given in the question, we can draw a direction diagram.



From the above diagram, it is clear that Gopal is walking in South direction.

63. (d)



So, no conclusion follows.

64. (d) 8, 6, 9, 23, 87?

The pattern is as follows

$$\begin{aligned} 8 \times 1 - 2 &= 6 \\ 6 \times 2 - 3 &= 9 \\ 9 \times 3 - 4 &= 23 \\ 23 \times 4 - 5 &= 87 \\ 87 \times 5 - 6 &= 429 \end{aligned}$$

So, the next term will be 429.

65. (a) Suppose, the number of questions in group A, B and C be x, y, and z, respectively.

Then,  $x + y + z = 100$  (given)

Total marks would be  $x + 2y + 3z$

Given,  $y = 23$

Total marks from section B = 46

Different possible values for z are 1, 2, 3, ....

∴ Corresponding values for x are 76, 75, 74, ...

(Since, total questions are 100)

when  $z = 1$ ,  $x = 76$ ,  $y = 23$

Total marks from groups A, B and C are 76, 46, 3 respectively.

$$\begin{aligned} \text{Percentage marks from A} &= \frac{76}{76 + 46 + 3} \\ &= \frac{76}{125} > 60\% \end{aligned}$$

when  $z = 2$ ,  $x = 75$ ,  $y = 23$

$$\begin{aligned} \text{Percentage marks from A} &= \frac{75}{75 + 46 + 6} \\ &= \frac{75}{127} < 60\% \end{aligned}$$

For all other values, when z increases, x decreases and contribution of marks from A keeps decreasing.

∴ There is only 1 possible value for questions from group C.

66. (a) Given,  $++ \rightarrow +$

$$- \rightarrow +$$

$$\times \rightarrow -$$

$$+ \rightarrow \times$$

Then,

$$\begin{aligned} & \frac{(36 \times 4) - 8 \times 4}{4 + 8 \times 2 + 16 + 1} \\ &= \frac{(36 - 4) + 8 - 4}{4 \times 8 - 2 \times 16 + 1} \\ &= \frac{(32) + 8 - 4}{4 \times 8 - 2 \times 16 + 1} \\ &= \frac{4 - 4}{4 \times 8 - 2 \times 16 + 1} = 0 \end{aligned}$$

67. (c) In the word CYBERNETICS,

I occupies the same position as it does in the English alphabet. The place value of 'I' is 9.

68. (c) Here,  $2^{31}$  is divided by 5

$$\begin{aligned} 2^{31} &= 2^{30} \times 2^1 \\ &= (2^2)^{15} \times 2 \\ &= (4)^{15} \times 2 \\ &= (-1 + 5) \times 2 = 4 \times 2 = 8 + 5 = 3 \end{aligned}$$





**Solutions [Q. Nos. 69 to 70]**

A N B O C P D Q E R F S G I H J V K X L Y M Z

69. (c) 7th letter from the left is D and 3rd letter to the right of D would be 'R'.

70. (b) The eighteenth letter from the beginning is V and fifteenth letter from the last is S. So, H will be exactly in between S and V.

71. (b) Here 

4	5	5
---	---	---

 is fixed.

So, total 3 digits number divisible by 5  
 $= 5 \times 4 \times 1 = 20$

72. (a) Here,

We have, to find LCM of 78 paise, 69 paise and 101 paise.

And,

$$78 = 1 \times 50 + 2 \times 10 + 2 \times 4 = 5 \text{ coins}$$

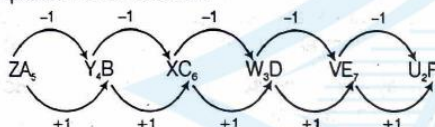
$$69 = 1 \times 50 + 1 \times 10 + 1 \times 5 + 2 \times 2 = 5$$

$$101 = 1 \times 101 = 1 \times 50 + 4 \times 10 + 1 \times 5 + 3 \times 2 = 9$$

$$\text{So, LCM} = 2 \times 3 \times 13 \times 23 \times 101 = 181194$$

73. (c)  $ZA_5, Y_4B, XC_6, W_3D, VE_7, U_2F$  --

The pattern is as follows :



So,  $VE_7$  and  $U_2F$  will be fit in the blanks.

74. (d) 61, 52, 63, 94 ?

The number formed by reversing the digit of each number of the sequence is square of consecutive natural numbers starting from 4. See how,

$$61 \dots 16 = 4^2$$

$$52 \dots 25 = 5^2$$

$$63 \dots 36 = 6^2$$

$$94 \dots 49 = 7^2$$

Therefore, the required number  $= 8^2 = 64 = 46$ .

75. (d) From the given information

Wife	Husband
X	A (Lawyer)
Y	B (Doctor)
Z	C (Engineer)

From the above table, no statement is correct.

76. (d) From the statements,

A is placed below E

E
A

C is placed below D

D
C

B is placed below A

A
B

D is placed between A and E, then

E
D
A
B
C

So, E will be on the top.

77. (c) Given that

B is taller than E but shorter than D.

$$D > B > E$$

A is shorter than C but taller than D.

$$D < A < C$$

Then the order is

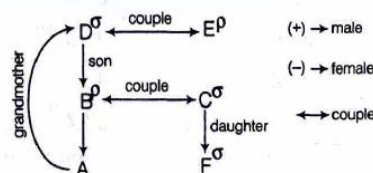
$$C > A > D > B > E$$

$$1 \quad 2 \quad 3 \quad 4 \quad 5$$

So, B is fourth.

**Solutions [Q. Nos. 78 to 81]**

From the given information in the question, we can draw a relation diagram,



78. (c) 'C' is the mother of A

79. (d) It cannot be determined because the gender of A is not defined.





3. 'Send down' means to dispatch somebody to some place or a lower level.

Hence, 'Send down a criminal' seems appropriate.

4. 'Send off a footballer' is also appropriate.

Hence, option 'b' is the best answer.

100. (b) The passive voice of 'can/may/might+first form of verb' is done as 'can/may/might+be+third form of the verb'.

Hence, the passive voice of the given sentence will be "These kittens can be played with safely (by you)."

101. (b) 'Aborigines' means the individuals belonging to or originating from the indigenous or the oldest known population or a place.

Hence, 'b' is the correct option.

102. (a) 'Exuberant' means 'full of unrestrained energy or joy'.

'Excited' and 'Poignant' have the similar meanings.

But 'Poignant' is usually meant for deep emotions of pity or sorrow.

Hence, 'a' is the best option.

103. (b) 'Affluence' means 'richness'.

Its opposite words are 'poverty' and 'misery'. But the latter is the extreme form of the former.

Hence, 'b' is the best option.

104. (a) It is clear from the sentence 'These mercenaries lived by the cult of the sword, worshipping athletic prowess and martial skills'.

105. (c) It is clear from the passage that the soldiers were loyal and fearless.

106. (b) It is clear from the sentence, 'It became fashionable for them to live sparse and frugal lives.....'.

107. (c) The correct sentence will be "I enclose a postal order which will cover the price of books and the postage."

108. (b) The correct option is (b).

109. (a) The preposition 'to' is always used with the word 'antidote'.

110. (d) The correct spelling is 'innovations'.

111. (d) 37 H means  $(00110111)_2$

17 H means  $(00010111)_2$

Now, we convert 37H, 17H binary number into decimal number.

$(00110111)_2$  decimal number =  $(55)_{10}$

$(00010111)_2$  decimal number =  $(23)_{10}$

$(55)_{10} + (23)_{10} = 23 \times 55(2) = (9)_{10}$

$\frac{46}{9} \text{ or } (1001)_2$

$(1001)_2$  Hexadecimal = 09, remainder = 09H

On division of 37H by 17H the remainder is 09H.

112. (b) If there are  $p$  possibilities for choice 1 and  $q$  possibilities for choice 2, then there are a total of  $p \times q$  different way of doing both. It is trivial that this can be extended to  $n$  choices.

So, there would be  $2^n$  boolean functions.

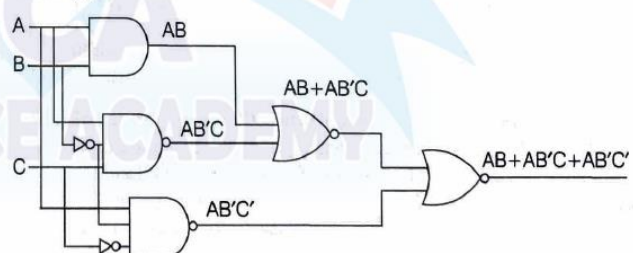
113. (b)

Binary	$h$	$h_3 h_2 h_1 h_0$	$(n+1) \bmod 16$	$g_3 g_2 g_1 g_0$
0000	0	0000	1	0001
0001	1	0001	2	0011
0010	2	0011	3	0010
0011	3	0010	4	0110
0100	4	0110	5	0111
0101	5	0111	6	0101
0110	6	0101	7	0100
0111	7	0100	8	1100
1000	8	1100	9	1101
1001	9	1101	10	1111
1010	10	1111	11	1110
1011	11	1110	12	1010
1100	12	1010	13	1011
1101	13	1011	14	1001
1110	14	1001	15	1000
1111	15	1000	0	0000

This gives the solution option (b).

$g_1(h_3 h_2 h_1 h_0) = \Sigma(4, 9, 10, 11, 12, 13, 14, 15)$

114. (b)



As, we can see in Logic Gates,

There are two NAND required.

115. (d) The diffraction beam can be machine read by a reading device which produces a reading light beam directed at the grating. The reading device has a plurality of detectors positioned to be illuminated by the diffracted light beam. Information can be stored in the optical memory by locally changing the optional properties of the grating.



116. (a)  $P = (F87B)_{16} = 1111100001111011$

2's complement =  $1111100001111011$

$$\begin{array}{r} \phantom{00000} \phantom{11110000101} \\ \phantom{00000} \phantom{11110000101} + 1 \\ \hline 0000011110000101 \\ (0000 \quad 1 \quad 1 \quad 1 \quad 1 \quad 0 \quad 0 \quad 0 \quad 1 \quad 0 \quad 1)_2 \\ \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\ 1024 \quad 512 \quad 256 \quad 128 \quad 64 \quad 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1 \end{array}$$

Value in decimal is  $(1925)_{10}$ . Hence,  $P = -1925$

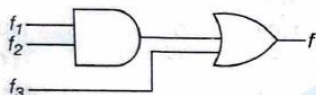
So, now doing  $8^* P = (-15400)_{10}$

Since, a negative number we have to find the 2's complement of  $-15400$ .

Binary of  $15400 = 0011 \ 1100 \ 0010 \ 1000$

2's complement =  $1100 \ 0011 \ 1101 \ 1000$   
 $\begin{array}{cccc} \text{C} & 3 & \text{D} & 8 \end{array}$   
 $= (C3D8)_{16}$

117. (c)



From the diagram

$$\begin{aligned} f &= f_1 f_2 + f_3 \quad (\text{put value}) \\ &= (4, 5, 6, 7, 8) f_2 + (1, 6, 15) = (1, 6, 8, 15) \end{aligned}$$

Now, as you know that the number 0, 1, 2, ..., 14, 15 represent the minterms like  $\Sigma_m(6, 8)$ .

- (i) If you AND (4, 6) with (4, 5, 6, 7, 8) it will result in (4, 6) but we don't need 4, so option (a) is wrong.

- (ii) If you AND (4, 8) with (4, 5, 6, 7, 8) it will result in (4, 8) but we don't need 4, so option (b) is wrong.

- (iii) If you AND (4, 6, 8) with (4, 5, 6, 7, 8) it will result in (4, 6, 8) but we don't need 4 here too, so option (d) is wrong.

- (iv) If you AND (6, 8) with (4, 5, 6, 7, 8) it will result in (6, 8) now when OR (6, 8) with (1, 6, 15), you get (1, 6, 8, 15) which is  $f$ , so option (c) is correct

118. (d) Given, expression  $\overline{(x + y + \bar{z})}$

As, we know De-morgan's law says

$$\overline{a + b} = \bar{a} \cdot \bar{b}$$

So, let

$$x + y = a$$

$$z = b$$

$$\Rightarrow \overline{(x + y + \bar{z})} = \overline{x + y} \cdot \bar{\bar{z}}$$

$$\begin{array}{ccc} \downarrow & \downarrow & \downarrow \downarrow \\ \overline{a + b} & & \bar{\bar{a}} \cdot \bar{\bar{b}} \end{array}$$

$$\Rightarrow \overline{x + y} \cdot \bar{\bar{z}} = (x + y) \cdot z$$

Hence,

$$\overline{x + y + \bar{z}} = (x + y) \cdot z$$

119. (c) Since,  $q \rightarrow s$  and  $r \rightarrow s$ , thus

$(q \vee r) \rightarrow s$ ;  $p \rightarrow (q \vee r)$  is given, then by rule of 'Syllogism',  $p \rightarrow s$  is deduced.

120. (a) Dynamic random access memories (DRAMs) are semiconductor integrated circuits (ICs) that operate like a bank of capacitors. DRAM consist atleast 1 MOS transistor necessarily.



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